

PHYS 112 HW3

Garrett Hedberg

No.

Date

Qs 1, 5 Ps 1, 2, 4, 5, 7, 13, 17, 18, 19, 22, 28, 33, 39, 45, 52

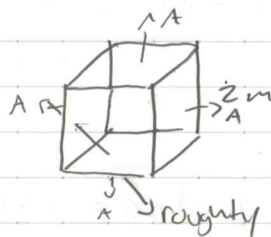
1) a) $\vec{\Phi} = \vec{E} \cdot \vec{A} = (8\hat{i} + 0\hat{j})$ b) $\vec{\Phi} = \vec{E} \cdot \vec{A} = (0\hat{i} + 12\hat{j})$ $\vec{E} = 4\hat{i}/4\hat{j}$ $\vec{A} = (2\hat{i} + 3\hat{j})$

5) $\epsilon = \frac{\sigma}{2\epsilon_0}$ $ma = E \cdot q$ $E_1 = \frac{2\epsilon}{\epsilon_0} + \frac{2\epsilon}{\epsilon_0} = \frac{4\epsilon}{\epsilon_0}$ $E_2 = \frac{2\epsilon}{2\epsilon_0} + \frac{\epsilon}{2\epsilon_0} = \frac{4\epsilon}{\epsilon_0}$ $E_3 = \frac{3\epsilon}{2\epsilon_0} + \frac{5\epsilon}{2\epsilon_0} = \frac{4\epsilon}{\epsilon_0}$

$E_1 = E_2 = E_3$ so a is same for all.

1) $E = 1800 \text{ N/C}$ $s = 3.2 \text{ mm}$ $\theta = 35^\circ$ $\Phi = -E \cdot A \cdot \cos(35) = -1.51 \text{e-}2 \text{ Nm}^2/\text{C}$
 $A = s^2 = 1.024 \text{e-}5 \text{ m}^2$

$\Phi = -1.51 \text{e-}2 \text{ Nm}^2/\text{C}$



$A = 4 \text{ m}^2$ $A_{\text{top}} = 0\hat{i} + 4\hat{j}$
 $A_{\text{bot}} = 0\hat{i} - 4\hat{j}$
 $A_{\text{left}} = -4\hat{i} + 0\hat{j}$

2) $\vec{E} = 4\hat{i} - 3(y^2 + z^2)\hat{j}$

a) Top has constant y so

$\vec{E}_{\text{top}} = 4\hat{i} - 18\hat{j}$
 $\Phi_{\text{top}} = \vec{E}_{\text{top}} \cdot \vec{A}_{\text{top}} = 0\hat{i} - 72\hat{j}$

b) Bottom has constant y so

$\vec{E}_{\text{bot}} = 4\hat{i} - 6\hat{j}$
 $\Phi_{\text{bot}} = \vec{E}_{\text{bot}} \cdot \vec{A}_{\text{bot}} = 0\hat{i} + 24\hat{j}$

c) A has no y component so doesn't matter

$\Phi = \vec{E} \cdot \vec{A}_1 = -16\hat{i} + 0\hat{j}$

d) no lines in z -axis so

$\Phi_{\text{back}} = 0$

e) $\sum \Phi = \Phi_{\text{top}} + \Phi_{\text{bot}} + \Phi_{\text{left}} + \Phi_{\text{right}} + \Phi_{\text{front}} + \Phi_{\text{back}}$
 $= (0\hat{i} - 72\hat{j}) + (0\hat{i} + 24\hat{j})$
 $\Phi_{\text{total}} = (0\hat{i} - 48\hat{j})$

a) $-72 \text{ Nm}^2/\text{C}$
 b) $24 \text{ Nm}^2/\text{C}$
 c) $-16 \text{ Nm}^2/\text{C}$
 d) $0 \text{ Nm}^2/\text{C}$
 e) $-48 \text{ Nm}^2/\text{C}$

$\Phi_{\text{left}} = -\Phi_{\text{right}}$

4) $E = 3 \text{e-}3 \text{ N/C}$ $a = 11 \text{ cm}$

$A = \pi r^2 = 3.8 \text{e-}2 \text{ m}^2$

$\Phi = E \cdot A = 1.14 \text{e-}4 \text{ Nm}^2/\text{C}$

$\Phi = 1.14 \text{e-}4 \text{ Nm}^2/\text{C}$

5) $q = +e$

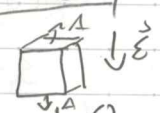


$A = d^2$

$\Phi = E \cdot A = \frac{q}{\epsilon_0}$ one face is $\frac{1}{6}$ so $\frac{q}{6\epsilon_0} = 3.02 \text{e-}9 \text{ Nm}^2/\text{C}$

$3.02 \text{e-}9 \text{ Nm}^2/\text{C}$

$$7) \Phi = \frac{q}{\epsilon_0} \quad q = 1.8 \mu C \quad \Phi = \frac{1.8 \mu C}{\epsilon_0} = \boxed{2.0 \text{ eSNm}^2/\text{C}}$$

13) @ 300m $E = 60 \text{ N/C}$ @ 200m $E = 100 \text{ N/C}$  $A = 10000 \text{ m}^2$ $\Phi = \frac{q}{\epsilon_0}$
Field is vertical so front, back and sides are 0 $\Phi \cdot \epsilon_0 = q$

$$\Phi_T = E_T \cdot A = -60 \text{ N/C} \cdot 10000 \text{ m}^2 = -6 \text{ eSNm}^2/\text{C}$$

$$\Phi_B = E_B \cdot A = -100 \text{ N/C} \cdot 10000 \text{ m}^2 = -1 \text{ e6 Nm}^2/\text{C}$$

$$q_T = \Phi_T \cdot \epsilon_0 = -5.3 \text{ e-6 C}$$

$$q_B = \Phi_B \cdot \epsilon_0 = 8.85 \text{ e-6 C}$$

$$q_{\text{tot}} = q_T + q_B = 3.54 \text{ e-6 C}$$

$$17) \sigma = 8.1 \text{ e-6 C/m}^2 \quad d = 1.2 \text{ m}$$

$$r = 0.6 \text{ m}$$

$$a) A = 4\pi r^2 = 4.5 \text{ m}^2$$

$$q = A \cdot \sigma = 3.66 \text{ e-5 C}$$

$$b) \Phi = \frac{q}{\epsilon_0} = \boxed{4.14 \text{ e6 Nm}^2/\text{C}}$$

$$18) \Phi = EA = \frac{q}{\epsilon_0} \quad \sigma = \frac{q}{A} \quad E \cdot \epsilon_0 = \frac{q}{A} = \sigma \quad E = 2.3 \text{ e5}$$

$$\sigma = 2.21 \text{ e-6 C/m}^2$$

$$19) \Phi = EA = \frac{q}{\epsilon_0} \quad q = 2.4 \text{ e-6 C} \quad r = 0.65 \text{ m} \quad A = 4\pi r^2 = 5.31 \text{ m}^2 \quad \sigma = \frac{q}{A}$$

$$a) \sigma = 4.52 \text{ e-7 C/m}^2$$

$$b) E = \frac{q}{A\epsilon_0} = \frac{\sigma}{\epsilon_0} = \boxed{5.11 \text{ e4 N/C}}$$

$$22) q = e \quad \lambda = 6 \text{ e-6 C/m} \quad F_e = E \cdot q = ma \quad \bar{\Phi} = Ed = \frac{q}{\epsilon_0} \quad \lambda = \frac{q}{L}$$

$$E = 2k \cdot \frac{6 \text{ e-6}}{0.06} = 1.798 \text{ e6 N/C}$$



$$\Phi = EA = \frac{q}{\epsilon_0}$$

$$\text{mass of electron} = 9.11 \text{ e-31 kg}$$

$$E = 2k \frac{q}{r}$$

$$F_e = E \cdot q = ma$$

$$\frac{E \cdot q}{m} = a$$

$$a = 3.16 \text{ m/s}^2$$

$$28) \lambda = 2 \text{ e-9 C/m} \quad r_1 = 5 \text{ cm} \quad r_2 = 10 \text{ cm} \quad r_3 = 15 \text{ cm}$$

$$a) E = 2k \frac{\lambda}{r} = \boxed{239.7 \text{ N/C}}$$

$$b) E \cdot \epsilon_0 = \sigma \quad E = 2k \frac{\lambda}{r} = 7.19 \text{ e2}$$

$$\sigma = -6.37 \text{ e-9 C/m}^2$$

$$c) E \cdot \epsilon_0 = \sigma \quad E = 2k \frac{\lambda}{r} = 3.596 \text{ e2 N/C}$$

$$\sigma = 3.18 \text{ e-9 C/m}^2$$

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33) $\sigma = 7e-22 \text{ C/m}^2$

a) it is $\boxed{0}$ because the charges are on the insideb) $\boxed{0}$ same reasoning

c) $\Phi = \epsilon A = \frac{q}{\epsilon_0}$

$\epsilon \cdot \epsilon_0 = \sigma$

$\epsilon = \frac{\sigma}{\epsilon_0}$

$\epsilon = 7.91e-11 \text{ NC}$

$\boxed{\epsilon = 7.91e-11 \text{ N/C}}$

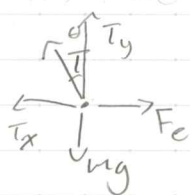
39) $m = 1 \text{ mg}$ $q = 2e-8 \text{ C}$ $\theta = 30$

$T_x = \epsilon \cdot q$

$\epsilon = \frac{\sigma}{2\epsilon_0}$

$T_y = \frac{\sigma}{2\epsilon_0} q$

$\frac{2T_x \epsilon_0}{q} = \boxed{\epsilon = 5.01e-9}$



$T_y = T \cos \theta$ $T = \frac{T_y}{\cos \theta}$

$T_x = T \sin \theta$ $T = 1.13e-5 \text{ N}$

$T_x = 5.66e-6 \text{ N}$

$T_x = F_e$ $T_y = mg$

$T_y = 1 \text{ mg} \cdot 9.8 \text{ m/s}^2$

$T_y = 9.8e-6 \text{ N}$

45) $\Phi = \epsilon A = \frac{q}{\epsilon_0}$ $r_1 = 10 \text{ cm}$ $r_2 = 15 \text{ cm}$ $r_3 = 12 \text{ cm}$ $r_4 = 20 \text{ cm}$ $Q_i = 4e-8$ $Q_o = 2e-8$

$A_1 = 4\pi r_1^2 = 0.126 \text{ m}^2$ $A_o = 4\pi r_2^2 = 0.283 \text{ m}^2$

$\sigma_i = \frac{Q_i}{A_1} = 3.18e-7 \text{ C/m}^2$ $\sigma_o = 7.07e-8 \text{ C/m}^2$

a) $\epsilon = k \frac{Q_i}{r_1^2} = \boxed{2.50e4 \text{ N/C}}$

b) $\epsilon = k \frac{Q_T}{r_2^2} = \boxed{1.35e4 \text{ N/C}}$ $Q_T = Q_i + Q_o = 6e-8$

52) $\rho = 1.84e-9 \text{ C/m}^3$ $a = 10 \text{ cm}$ $b = 20 \text{ cm}$

a) $\boxed{0}$ within shellb) $\boxed{0}$ within the shellc) $\boxed{0}$ still within the shell

d) $r = 1.5a = 15 \text{ cm}$
 $\boxed{7.31 \text{ N/C}}$

$V = \frac{4}{3}\pi(0.15^3 - \frac{4}{3}\pi 0.1^3) = 9.95e-3 \text{ m}^3$

$Q = \rho \cdot V = 1.83e-11 \text{ C}$

$\epsilon = k \frac{Q}{r^2} = 7.31 \text{ N/C}$

e) $r = b = 20 \text{ cm}$

$V = \frac{4}{3}\pi(r^3 - a^3) = 2.93e-2 \text{ m}^3$

$Q = \rho \cdot V = 5.40e-11 \text{ C}$

$\epsilon = k \frac{Q}{r^2} = \boxed{12.1 \text{ N/C}}$

f) $r = 3b = 60 \text{ cm}$

$V = \frac{4}{3}\pi(b^3 - a^3) = 2.93e-2 \text{ m}^3$

$Q = \rho \cdot V = 5.40e-11$

$\epsilon = k \frac{Q}{r^2} = \boxed{1.35 \text{ N/C}}$